A COMPREHENSIVE APPROACH TO ENHANCING THE RESILIENCE OF INFORMATION SYSTEMS: FROM MATHEMATICAL MODELING TO RISK MANAGEMENT STRATEGIES

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This article discusses the issue of improving the reliability of information systems. The main focus is on mathematical analysis methods used to assess fault tolerance in data exchange systems. In the modern world, when data is becoming an increasingly valuable asset, the importance of reliability of information systems cannot be overestimated. The research focuses on the development of a mathematical model, which is presented in the form of a graph of states and failure probabilities, and also includes a set of differential equations to describe the dynamics of the system. This model is designed to operate at three levels, which allows you to analyze in detail various aspects of the functioning of the system and identify potential threats at each stage.

The solution of the proposed equations allows not only to determine the probability of failures at different points in time, but also provides tools for effective troubleshooting. Thus, the implementation of the proposed approach contributes to improving the overall reliability of systems, reduces the risks of critical failures, and improves infrastructure management. The article also discusses the possibilities of practical application of the developed model in various types of information systems, including critical infrastructures, where a high level of reliability is absolutely necessary.

Keywords: information system, diagnostics of network parameters, network resources reliability, failure, network operation level.
В данной статье рассматривается вопрос повышения надежности информационных систем. Основное внимание уделяется методам математического анализа, применяемым для оценки устойчивости к сбоям в системах обмена данными. В условиях современного мира, когда данные становятся все более ценным активом, важность надежности информационных систем не может быть переоценена. Исследование фокусируется на разработке математической модели, которая представлена в виде графика состояний и вероятностей отказов, а также включает комплекс дифференциальных уравнений для описания динамики системы. Эта модель разработана для функционирования на трех уровнях, что позволяет детально анализировать различные аспекты функционирования системы и идентифицировать потенциальные угрозы на каждом из этапов.

Решение предложенных уравнений позволяет не только определить вероятности возникновения сбоев в разные моменты времени, но и предоставляет инструменты для эффективного выявления и устранения неисправностей. Таким образом, внедрение предложенного подхода способствует повышению общей надежности систем, снижает риски возникновения критических отказов, и улучшает управление инфраструктурой. В статье также обсуждаются возможности практического применения разработанной модели в различных типах информационных систем, включая критически важные инфраструктуры, где высокий уровень надежности является абсолютно необходимым.

**Ключевые слова:** информационная система, диагностика параметров сети, надежность сетевых ресурсов, отказы, уровень функционирования сети.

**Introduction.** In the modern world, where information technology plays a leading role in various spheres of human activity, the reliability of information systems becomes a critically important aspect. These systems form the basis for data transmission, processing, and storage, and any malfunctions in their operation can lead to serious consequences, including data loss, reduced productivity, and even critical emergency situations in vital infrastructures. Therefore, enhancing the resilience of information systems to failures and malfunctions is a priority task for specialists in the field of information technology.

The problem of information system reliability is multifaceted and requires a comprehensive approach to its solution. In recent years, methods of mathematical modeling have been actively developed, allowing the analysis and prediction of system behavior under various external and internal influences. The application of these methods opens new possibilities for assessing fault tolerance and developing effective strategies to enhance the reliability of information systems.

This article proposes an innovative method for assessing the resilience of information systems to failures, based on mathematical modeling. The method includes the development of a mathematical model, which is a graph of states and failure probabilities, as well as a system of differential equations for its description. This model allows for the identification of potential vulnerabilities in the structure and functioning of information systems, as well as aids in the development of measures to eliminate them. The solution of the proposed model provides quantitative estimates of failure probabilities at various levels of system operation, which is a key element in ensuring its reliability.

The article is organized as follows: after an introduction that outlines the relevance of the problem...
and the goals of the research, a literature review reflects the current state of the issue of assessing the reliability of information systems. The methodology for developing the mathematical model, the main stages of its creation, and the principles of operation are then described. The results section presents the data obtained during the modeling and their analysis. The conclusion summarizes the findings of the research and outlines prospects for further work in this area.

**Materials and methods.** To assess the resilience of information systems to failures, methods of mathematical analysis and mathematical modeling were used, including the development of a state graph and failure probabilities, as well as a system of differential equations for analyzing and optimizing the functioning of systems across three levels: data transmission, processing, and storage. This allowed for the prediction of failure probabilities and the identification of critical points to enhance system reliability.

**Literature Review.** Extensive research has been conducted in the field of hardware protection against malfunctions and system security, presented in a series of key articles. One of the innovative developments is S-DETECTOR, introduced in [1], which is an implementation of DETECTOR with selective protection of vulnerable registers. This approach significantly enhances performance and also reduces the damage that could be caused by failure coverage.

In the field of electric vehicles, a collision prevention system is actively being developed, introduced in [2]. This method is innovative due to the use of embedded real-time subsystems at the hardware level, providing reliable protection against potential faults.

The fundamental methodology for designing fault-tolerant microprocessor systems, described in [3], is based on software-implementable hardware fault tolerance. This methodology represents an important step towards creating systems capable of effectively dealing with potential malfunctions and ensuring reliable operation.

Article [4] proposes an extension of the scheduling theory for mixed-criticality systems, taking into account temporal faults. These extensions, which introduce the concept of discard relations generalizing the notion of criticality, aim to improve the schedulability analysis and the control of dependencies between tasks, facilitating effective system resource management and enhancing reliability in the face of temporal faults.

Experimental data presented in [5] demonstrate that the Defender architecture for a fault-tolerant router in a network-on-chip successfully ensures resilience to permanent faults. Other studies, such as the use of approximate computations to reduce energy consumption in deep neural network accelerators [6] and a design methodology for enhancing the fault tolerance of deep learning models using neuromorphic hardware [8], also make significant contributions to the field of hardware protection.

Furthermore, article [7] examines the Defender architecture for a fault-tolerant router in a network-on-chip, marking an important step in ensuring resilience to permanent faults in modern network systems.

In the context of secure multicast in networks with interceptors, article [9] explores the issue and develops methods for ensuring security in environments with multiple sources.

Detailed studies, such as proving security for the two-message signed Diffie-Hellman key exchange protocol [10], and the extended mechanism for ensuring integrity and predictability in intra-chip communication during random hardware faults (AIQ) [11], provide a deep analysis and development of tools for cybersecurity in modern computing environments.

A review of contemporary trends in access control in the Internet of Things (IoT) [12] makes an important contribution to understanding security in the realm of device and system interactions in the IoT.

Research such as the use of CSP process algebra and the PAT tool for analyzing the Apache Kafka messaging mechanism [13], as well as a review of the security of existing Digital Signature Schemes (DSS) in the context of the strong existential unforgeability under chosen message attack model (sEUF-CMA) [14], provide valuable knowledge for ensuring security in the realms of data exchange and signatures.

Considering the advancement of modern technologies, studies on the application of a new protocol with a guaranteed error of $O(1/\varepsilon)$ for pure differential privacy [15] and examining the security of the Signal messenger with a proposal for an improved protocol SAID [16] offer new perspectives and solutions for secure data transmission and communications.

Finally, research in the field of distributed systems, such as a Configurable Distributed System for Verification and Launch (CDCLS) for aerospace vehicles [17] and the proposal of the DepFast library [18], are significant steps in the field of ensuring...
fault tolerance and efficient resource management in modern distributed systems [19].

This literature review also addresses issues of processing large volumes of data in intelligent transportation using mobile edge computing technology [20]. Challenges related to efficient data management and processing in transportation systems are becoming increasingly relevant, and this research suggests approaches to addressing these challenges based on the use of mobile computing.

Additionally, considering a secure data transmission mechanism in ad hoc mobile networks [21] is an important part of the review. Ensuring secure data transmission in ad hoc networks, where devices interact without a centralized infrastructure, is a complex task, and this article suggests approaches to ensuring confidentiality and integrity of data in such networks.

Research on Scalable Multilevel Distributed Coding (SMDC) for encoding independent information messages with different reliability requirements [22] also contributes to the discussion on fault tolerance and security. This approach can be useful for transmitting information under conditions where different messages have varying reliability requirements.

In conclusion, introducing a new steganography model - the Cover Processing-based Steganographic Model (CPSM) [23] - complements the discussion on innovative approaches to ensuring confidentiality and security of information messages. This model offers new ways of embedding and protecting information, making it significant in the context of developing secure messaging systems.

**Modeling Object.** The object of modeling in the scientific article presented is information systems designed to ensure the transmission, processing, and storage of data in various areas of human activity. Particular attention is paid to data transmission systems operating under increased reliability and fault tolerance requirements. The study aims to analyze and assess the resilience of these systems to potential failures and malfunctions that may arise due to various external and internal impacts.

As a specific object of modeling, information systems with a three-level operating architecture are chosen, including data transmission, data processing, and data storage levels. This structure reflects the complexity and hierarchy of modern information systems and allows for considering various scenarios of system component interactions and their impact on overall reliability.

A mathematical model based on graph theory and probability theory principles has been developed to analyze the fault tolerance of information systems. The model is a state graph, each state corresponding to a certain level of system operation, and transition probabilities between these states, reflecting the likelihood of system component failures and their impact on overall operability. A system of differential equations is used to describe the dynamics of system state changes, the solution of which allows estimating the probabilities of the system being in each of the possible states over time.

### Table 1 - Important components of Information systems (IS)

<table>
<thead>
<tr>
<th>№</th>
<th>Component</th>
<th>Function</th>
<th>Criticality Level</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Database Server</td>
<td>Data storage, management, and processing</td>
<td>High</td>
</tr>
<tr>
<td>2</td>
<td>Communication Equipment</td>
<td>Ensuring data transmission between network devices</td>
<td>Medium</td>
</tr>
<tr>
<td>3</td>
<td>Application Server</td>
<td>Running business applications and services</td>
<td>High</td>
</tr>
<tr>
<td>4</td>
<td>Data Storage Systems</td>
<td>Centralized storage of large volumes of data</td>
<td>High</td>
</tr>
<tr>
<td>5</td>
<td>Backup Systems</td>
<td>Data recovery after failures</td>
<td>High</td>
</tr>
<tr>
<td>6</td>
<td>Network Routers and Switches</td>
<td>Traffic routing and network flow management</td>
<td>Medium</td>
</tr>
<tr>
<td>7</td>
<td>Security Systems (Firewall, IDS/IPS)</td>
<td>Network protection against unauthorized access and attacks</td>
<td>High</td>
</tr>
<tr>
<td>8</td>
<td>Data Processing Centers (DPC)</td>
<td>Physical and software support of IT infrastructure</td>
<td>High</td>
</tr>
<tr>
<td>9</td>
<td>End-User Devices (PCs, Laptops)</td>
<td>User access to applications and data</td>
<td>Medium</td>
</tr>
<tr>
<td>10</td>
<td>Cloud Computing Services</td>
<td>Flexible scaling and resource provisioning</td>
<td>Medium</td>
</tr>
</tbody>
</table>
Modeling the fault tolerance of information systems using the proposed mathematical model enables the identification of the most vulnerable elements of the system, assess the risks of potential failures, and develop strategies to improve reliability and resilience to malfunctions. This approach ensures a higher level of information systems’ readiness for unforeseen situations, minimizes potential losses from failures and malfunctions, and improves the quality of service for end-users.

Table 1 presents the critically important components of information systems (IS), their main functions, and the level of criticality.

This classification emphasizes the importance of various IS components in ensuring their stable and reliable operation. Components with a high level of criticality require special attention in the context of developing measures to improve fault tolerance and ensure data security.

The functional state of an information system (IS) can be represented in accordance with Figure 1, where the efficiency of the IS is determined by its ability and readiness to perform basic functions, such as sending data packets and processing user requests. In contrast to efficient operation, an inefficient state of the IS is characterized by problems including delays, malfunctions, and complete failures. Additionally, within the scope of the study, various categories of errors that can lead to system failures can be identified, as detailed in Figure 2.

![Figure 1 - Characteristics of the functioning of the IS](image1)

![Figure 2 - Errors that can lead to failures](image2)

In the framework of system-technical analysis, information systems are considered as integrated structures consisting of interconnected and interacting levels. The key elements of such systems are system and application software, database management systems, as well as a set of functions and services responsible for data transmission, storage and processing (Figure 3).
When developing reliable and fault-tolerant information systems and networks, significant attention is dedicated to minimizing the time and resources required for the recovery and replacement of failed components. In light of this, the application of various modeling methods for selecting the optimal strategy for implementing backup elements, considering potential failures, becomes a highly sought-after approach.

The task of modeling and assessing the probabilities of failures in information systems acquires particular relevance, allowing for the identification of components that require modernization or replacement with backups. For addressing this task, it is appropriate to use the Markov chain methodology. This method is one of the most accessible and effective mathematical tools for modeling various operations, including failures in information systems, occurring as random processes.

Markov chains are an established mathematical tool for analyzing problems with a probabilistic nature. Such a chain is represented in the form of a graph, where vertices correspond to system states, and edges reflect the intensity of transitions between these states. Using an annotated graph, it is possible to determine the probabilities of the system being in each of the states both over time and in stationary conditions.

Before beginning modeling, initial parameters are defined, such as possible states of failures specific to the analyzed information system, and all potential connections between states are established in the form of event flow intensities that effectuate the system’s transitions from one state to another.

Then, based on the set parameters, one can proceed to create the model using graph methodology, based on the principles of Markov chain theory.

In the context of the analyzed information system, a failure is considered a stochastic process with a finite set of states, where events occur individually rather than en masse. This indicates the ordinariness of the studied model, which also assumes the absence of aftereffects. This means that the number of events occurring in any given time interval does not correlate with the number of events in any other non-overlapping interval.

In the process of building the model to assess network fault tolerance, it is assumed that a failure can occur at any level of its operation at any given time, including the local level, the network environment level, or the level of system's critically significant nodes (Figure 4).
In the process of developing a model and evaluating the characteristics of network fault tolerance, it is assumed that the information system at certain points in time may experience a failure at one of the levels of its functioning. These levels include: the local level, the network environment level, and the critical node level. Within the framework of modeling, it is assumed that the system can be in various failure states, designated as $S_{ij}$, where the index $i$ indicates the level of functioning (with three levels in this example), and the index $j$ classifies the type of failure (with five different types in this example).

The initial state of the system is assumed to be trouble-free, with fully functioning resources. All subsequent states differ from the initial one and are characterized by non-standard operation of the system in conditions of various failures.

Next, a graph of system states is constructed, which illustrates the transitions from each possible failure state at the appropriate level to a failure-free state, designated as $S_0$. In this graph, the vertices represent the possible states of the system, and the edges reflect the intensity of transitions between these states, denoted as $\lambda_i$.

To quantify fault tolerance and failure probabilities in the network, a mathematical model is formed based on the constructed graph of states. This model is expressed through a system of differential or linear algebraic equations, following the rule: on the left is the derivative of the probability of a state in time, and on the right is the sum of the products of the probabilities of states from which transitions to a given state occur, based on the intensity of the corresponding streams of events, minus the total intensity of the streams leading away from this state, multiplied by the probability of this state.
To assess the level of fault tolerance and find the probabilities of failures in the network according to a structured graph, we compile a mathematical model in the form of a system of differential or linear algebraic equations according to the following rule: on the left is the derivative of the probability of the state, and on the right is the sum of the products of the probabilities of those states from which the arrows go to this state, based on the intensity of the corresponding event flows, minus the total intensity of the flows leading from a given state multiplied by the probability of a given state.

To quantify the fault tolerance of the network and determine the probability of failures, a mathematical model based on the constructed graph of states is used. The model is presented in the form of a system of differential or linear algebraic equations, which are formulated as follows:

The left side of the equation contains the derivative of the probability of finding the system in a given state in time, which corresponds to the rate of change in the probability of this state.

The right side of the equation consists of two parts:

The first part includes the sum of the products of the probabilities of previous states on the intensity of the streams of events that transfer the system to this state. This reflects the contribution to the probability of a state from all possible previous states.

The second part is the product of the probability of the current state by the total intensity of the streams of events that bring the system out of this state. This expresses the loss of probability due to transitions to other states.

Thus, if we denote the probability of the $S_i$ state as $P(S_i)$ and the intensity of the transition from the $S_i$ state to the $S_j$ state as $\lambda_{ij}$, then for each $S_i$ state the equation will take the form:

$$\frac{dP(S_i)}{dt} = \sum_{j \neq i} P(S_j)\lambda_{ji} - P(S_i)\sum_{j \neq i} \lambda_{ij}$$

where $\frac{dP(S_i)}{dt}$ is the rate of change in the probability of the $S_i$ state over time, the first term sums up the contributions from all possible transitions to the $S_i$ state, and the second term subtracts the probability of leaving the $S_i$ state to all other states.

Solving this system of equations will allow us to find the probabilities of all states of the system at any given time or in a stationary mode, if we consider the long-term behavior of the system.

**Discussion.** In the framework of modern research, an analysis of the fault tolerance of information systems (IS) using the theory of Markov chains has been carried out. The central part of the work is the construction of an IC failure graph, which describes the probabilistic transitions between different states of the system, including states characterizing various levels of functioning and types of failures. Failure states in this context are divided into three main categories: the local level, the network environment level and the level of critical nodes, each of which, in turn, is associated with five types of failures, covering hardware, system, application problems, as well as failures of network devices and physical communication channels.

The study begins with determining the initial state of the system, assuming its full functionality without any failures. The subsequent analysis focuses on modeling the transitions of the system to failure states and back, using a mathematical model based on Markov circuits. This approach allows us to quantify the probabilities of each of the possible states of the system over time, which is a key aspect in studying and improving its fault tolerance.

In the course of the study, a system of differential and linear algebraic equations was developed, which allows us to calculate the dynamics of changes in the probabilities of system states based on the intensities of event flows leading to failures or restoration of functioning. The solution of this system of equations makes it possible to predict the behavior of the system in various operating conditions and under various failure scenarios.

One of the most important results of the work was the identification of key factors affecting the level of fault tolerance of the information system. In addition, the most vulnerable components and levels of functioning of the IC were identified, for which the risk of failure is maximum. This data can be used in the development of strategies to improve the reliability and fault tolerance of systems, as well as in planning measures to prevent failures or minimize their consequences.

**Results.** As part of the research, a mathematical model based on Markov chains was developed and tested to analyze the fault tolerance of information systems (IS). The model allowed us to estimate the probabilities of transitions between different states of the system, including normal operation and various failure levels associated with the local level, the level of the network environment and the level of critical nodes. The failure specification included hardware problems, system failures, application problems, failures of
network devices and physical communication channels.

The main results of the study can be summarized as follows:

Quantification of the probabilities of states - the probabilities of finding the system in each of the possible states were determined depending on the time and operating conditions. This made it possible to identify the most vulnerable components of the IC to failures and evaluate the effectiveness of various strategies to increase fault tolerance.

Identification of key fault tolerance factors - the study showed that the intensity and probability of failures significantly depend on the level of functioning of the system components and the type of possible failures. Identifying these dependencies allows you to focus efforts on eliminating the most significant vulnerabilities.

Analysis of the dynamics of changes in system states - the proposed approach made it possible to trace how the probability of finding a system in certain failure states changes over time, which contributes to a better understanding of the recovery processes after failures and planning preventive measures.

Development of recommendations to improve fault tolerance - based on the results obtained, recommendations were formulated to improve the architecture and configuration of information systems aimed at reducing the likelihood of failures and minimizing their consequences.

Thus, the results of this study make a significant contribution to the theory and practice of designing and operating fault-tolerant information systems. The use of mathematical modeling based on Markov chains allows for a more in-depth analysis of the processes taking place in the IP and the development of effective risk management strategies related to potential failures.

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